

# Brain Activity during a Visuospatial Working Memory Task Predicts Arithmetical Performance 2 Years Later

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**Visuospatial working memory (WM) capacity is highly correlated with mathematical reasoning abilities and can predict future development of arithmetical performance. Activity in the intraparietal sulcus (IPS) during visuospatial WM tasks correlates with interindividual differences in WM capacity. This region has also been implicated in numerical representation, and its structure and activity reflect arithmetical performance impairments (e.g., dyscalculia). We collected behavioral ( $N = 246$ ) and neuroimaging data ( $N = 46$ ) in a longitudinal sample to test whether IPS activity during a visuospatial WM task could provide more information than psychological testing alone and predict arithmetical performance 2 years later in healthy participants aged 6–16 years. Nonverbal reasoning and verbal and visuospatial WM measures were found to be independent predictors of arithmetical outcome. In addition, WM activation in the left IPS predicted arithmetical outcome independently of behavioral measures. A logistic model including both behavioral and imaging data showed improved sensitivity by correctly classifying more than twice as many children as poor arithmetical performers after 2 years than a model with behavioral measures only. These results demonstrate that neuroimaging data can provide useful information in addition to behavioral assessments and be used to improve the identification of individuals at risk of future low academic performance.**

**Keywords:** child development, fMRI, mathematics, numerical abilities, working memory

## Introduction

Of the various mathematical domains taught at school, number understanding, counting, and arithmetic are those in which cognitive theory and experimental methods are the most developed (Butterworth 2005). Arithmetic is an academic skill that relies on a range of cognitive processes (Dehaene et al. 2004). Poor arithmetical abilities are a serious handicap for individuals and for society in general, increasing the risk of unemployment and depression and significantly reducing lifetime earnings (Gross 2009). Children who have difficulties in arithmetic early on tend to remain low achievers (Andersson 2010). For this reason, finding early cognitive markers of individual differences in arithmetical abilities and their future development is a critical step for the implementation of successful intervention (Ramani and Siegler 2008; Holmes et al. 2009; Räsänen et al. 2009).

Behavioral studies have suggested that working memory (WM) could be one of the cognitive markers associated with arithmetical achievement (see Raghubar et al. 2010 for review). WM refers to a set of mental processes that enable us to hold and manipulate relevant information for brief periods of time.

WM capacity is correlated with arithmetical performance both in children with and without known learning difficulties (Henry and MacLean 2003; Kytälä et al. 2003; Maybery and Do 2003; Alloway et al. 2005, 2009; Geary et al. 2009; Meyer et al. 2010). WM measures can also predict future development of arithmetical ability (Jarvis and Gathercole 2003; Gersten et al. 2005; Bull et al. 2008; Alloway and Alloway 2010; but see Gathercole et al. 2003; Geary et al. 2009) above and beyond measures of general intelligence or reasoning abilities (Alloway TP and Alloway RG 2010).

A number of theoretical models of WM have been proposed, and these may differ in their potential use for the study of differences in arithmetical development (Berch 2008). Experimental studies typically make a distinction based on the type of information held in WM, whether it is verbal or visuospatial. The evidence is mixed regarding whether visuospatial or verbal WM has the most predictive value regarding the development of arithmetical abilities (Gathercole et al. 2003; Rasmussen and Bisanz 2005; Bull et al. 2008; Meyer et al. 2010) and whether WM and nonverbal reasoning have independent predictive values (Passolunghi et al. 2007; Alloway TP and Alloway RG 2010; Primi et al. 2010).

Arithmetical impairments, for example, in the case of developmental dyscalculia, may arise from deficits in elementary numerical processing such as impaired representation and processing of basic numerical magnitude, impaired numerosity coding or impaired “number sense” (see Butterworth 2005, 2010 for review). Meta-analyses have identified the intraparietal sulcus (IPS) as the locus of numerical representation (Dehaene et al. 2003; Cohen Kadosh et al. 2008). Both structure (Isaacs et al. 2001; Rotzer et al. 2008; Rykhlevskaia et al. 2009) and brain activity (Kucian et al. 2006; Price et al. 2007; Kaufmann et al. 2009; Rotzer et al. 2009; Mussolin et al. 2010) in this region reflect group differences in mathematical difficulties, and current research points to IPS abnormalities as the single biological marker of developmental dyscalculia (Rubinsten and Henik 2009; Butterworth 2010). Brain imaging data indicate that numerical and WM functions converge in the IPS (Zago and Tzourio-Mazoyer 2002; Zago et al. 2008), which shows WM activation across several stimulus presentation modalities (Linden 2007). Moreover, individual differences in activity in the IPS are correlated with WM capacity differences among adults (Todd and Marois 2005), as well as when comparing children and adults (Klingberg et al. 2002a; Crone et al. 2006).

In the present study, we first attempted to replicate previous findings regarding the predictive power of WM and reasoning measures for future arithmetical performance (Raghubar et al. 2010) using longitudinal data collected in a large sample of participants ranging in age from 6 to 16 years ( $N = 246$ ). This focus on a wide age range is novel compared with previous

studies, which tested single age groups (Gathercole et al. 2003; Bull et al. 2008; Alloway TP and Alloway RG 2010) or used age-corrected measures (Bull et al. 2008). Moreover, the inclusion of different age groups allowed us to investigate whether the relationship between predictive measures and arithmetical outcome changes with age. Because of the mixed evidence regarding whether visuospatial or verbal WM is most relevant to arithmetical abilities and of the value of recording multiple and varied measures, we assessed 3 behavioral measures of WM, which differed in terms of stimulus type: a verbal WM task with word stimuli, a verbal WM task with number stimuli, and a visuospatial WM task.

We first tested whether the different types of WM measures and nonverbal matrix reasoning contributed to prediction of arithmetical performance 2 years later. Arithmetical performance was assessed with grade-dependent tests of elementary arithmetic. Our second and main goal was to assess whether brain activity, measured as change in the blood oxygen level-dependent (BOLD) contrast, could improve prediction of arithmetical outcome. The hypothesis behind this analysis was that physiological measures would provide a more direct evaluation of the key neural substrates necessary for arithmetical performance. Whole-brain and local IPS activation during a visuospatial WM task was measured in a subset of 46 participants. Bilateral IPS regions of interests (ROIs) were defined using the results of a meta-analysis of numerical representation (Cohen Kadosh et al. 2008), and we separately assessed the predictive use of the left and right IPS ROIs.

## Materials and Methods

### Participants

Participants were healthy volunteers recruited using random sampling from the population registry in Nynäshamn in Sweden and part of a longitudinal study of typical development ("Brainchild" study, Söderqvist et al. 2010). Included here were participants aged between 6 and 16 years at the first time of testing (T1) who participated in the second round of testing (T2) 2 years later. The upper limit of the age range was chosen to only include participants in the educational system at T1 and T2.

Exclusion criteria were a diagnosed neuropsychological disorder other than attention deficit and hyperactivity disorder (ADHD) and dyslexia, a mother tongue other than Swedish, and severe hearing or vision impairment. We expected normal rates of these disorders in the population. ADHD symptoms corresponding to the American Psychiatric Association criteria (American Psychiatric Association, [Diagnostic and Statistical Manual of Mental Disorders -IV], 2000) were rated by parents for 223 of the 246 participants at T1. One child was rated as having more than 6 symptoms of hyperactivity; none was rated as having more than 6 symptoms of inattention. Informed consent was obtained from the participants and from the parents of children under 18. The study was approved by the local ethics committee of the Karolinska University Hospital, Stockholm.

### Behavioral Assessment

A total of 246 participants (125 males) participated in the behavioral assessment. The sample included participants aged 6 ( $N=42$ ), 8 ( $N=37$ ), 10 ( $N=46$ ), 12 ( $N=45$ ), 14 ( $N=40$ ), and 16 years ( $N=36$ ) at T1 (mean age: T1, 10.83 years [SD 3.33]; T2, 12.86 [3.36]). Participants completed a large neuropsychological battery administered individually in a quiet room. In a separate session, arithmetical achievement was measured by a written test performed individually in isolation or in a group.

### WM Measures

Visuospatial WM was assessed using the dot matrix task from the Automated Working Memory Assessment battery (Alloway 2007). This

task involves remembering the location and order of dots displayed sequentially in a grid on a computer screen. Verbal WM was assessed with a backwards digit recall task. Numbers were read aloud to the participants, who verbally repeated them in the reverse order. In both of these tests, difficulty was increased after 4 trials were correctly answered by adding one item to be remembered. The tests terminated when 3 errors were committed on one level. The scores used were the total number of correct trials. The third WM task was a 3-back task. Participants were read a total of twenty Swedish words and were asked to indicate, by responding yes or no on each trial, whether the word was the same as the word read 3 trials before. A score was calculated by subtracting the number of false alarms (wrong yes responses) from the number of correct responses. Although this task has not been validated and the data suggest poorer reliability than the other WM measures, it was included to obtain a measure of nonnumerical verbal WM.

### Reasoning Ability

Raven's Progressive Matrices were used as a measure of reasoning ability (Raven 1998). Participants in the youngest age group (6-year-olds) performed subtests A-D, while all other participants performed all subtests (A-E), each comprising 12 items. The test did not have a time limit, although if the participant did not give an answer within 1 min the administrator asked for an answer.

### Arithmetical Abilities

The arithmetical assessment was based on the Trends in Mathematics and Science Study (Martin et al. 2004) and Basic Number Screening Test (Gillham and Hesse 2001) and was designed in 4 school-grade-dependent versions (grades 2, 4, 6, and 8, suitable for 14- to 27-year-olds). Grades 2 and 4 problems included magnitude judgments, questions about the number sequence, as well as elementary arithmetic (addition, subtraction, division, multiplication, and fractions). Grades 6 and 8 problems included elementary arithmetic and elementary algebra (simple equations with variables). Items were piloted in second and sixth graders ( $N=400$ ) at 3 schools in a suburb of Stockholm. Testing time was 30 min.

### Preprocessing Analyses

The raw results of the arithmetical and reasoning tests were initially transformed into ability scores. This transformation was carried out by item response theory (IRT) analyses using a partial credit model. The ability score of the IRT analyses is a measure of the probability of a participant passing the test, a function of the difficulty level of the item and the ability of the participant (see Bergman Nutley et al. 2010 for details). These measures were then transformed into Z-scores. This preprocessing permitted combined analyses of different age groups, even though the groups did not perform the exact same tasks since the tests were age dependent.

### Brain Imaging

#### Data Collection

A subset of 46 participants (23 males) were randomly selected to participate in the imaging part of the study (Söderqvist et al. 2010). This sample included participants aged 6 ( $N=6$ ), 8 ( $N=9$ ), 10 ( $N=9$ ), 12 ( $N=6$ ), 14 ( $N=9$ ), and 16 years ( $N=7$ ) at T1 (overall mean age: T1, 10.96 [SD 3.35]; T2, 13.02 [3.35]). Magnetic resonance imaging (MRI) data were collected on a 1.5T Siemens scanner. T2\*-weighted functional images were acquired with a gradient-echo echo-planar imaging (EPI) pulse sequence with repetition time = 3000 ms, echo time = 50 ms, flip angle = 90°, 30 oblique slices, 4.5 mm slice thickness, 0.5 mm interslice distance, 220 × 220 mm field of view (FOV) and 64 × 64 grid, resulting in a voxel size of 3.44 × 3.44 × 4.5 mm. Structural T1-weighted spin echo images were acquired with a 3D magnetization prepared rapid gradient echo (MPRAGE) sequence (FOV = 256 × 256 mm, 256 × 256 grid, 1 mm<sup>3</sup> voxel size).

#### Functional MRI Paradigm

Participants performed a visuospatial WM grid task in two 5-min sessions including 16 WM and 16 control trials. Trial order was pseudorandomized. Stimuli were presented with E-Prime software

using an MRI-compatible visual system (NordicNeuroLab). Dots were presented sequentially in a  $4 \times 4$  grid for 500 ms, with 500-ms interval between dots. Two loads (2 dots or 4 dots) were implemented in the paradigm; 1500 ms after the last dot and the grid disappeared, a cue was presented in the grid for 3000 ms. The cue was a number referring to a serial position in the previous stimulus sequence. Participants indicated with a yes/no response (right index and middle finger responses, respectively) whether the number and its position in the grid matched, for example, “2?” would prompt the participant to indicate whether the second circle had appeared in the grid position filled by the number. In the control condition, the cue (number 8) always required a “no” response. A new sequence began 2000 ms after the response cue disappeared.

### Data Analysis

Preprocessing and statistical analyses (see Söderqvist et al. 2010) were carried out with SPM5 (<http://www.fil.ion.ucl.ac.uk/spm/software/spm5>). Separate boxcar regressors modeled correct trials of the WM and control load 2 and 4 conditions, with durations of 8 (load 2) or 10 s (load 4). These regressors were convolved with a canonical hemodynamic response function, its temporal and dispersion derivatives, and, together with regressors representing residual movement-related artifacts and the mean over scans, comprised the full model for each session. Parameter estimates calculated from the least-mean-squares fit of the model to the data were used in a pairwise contrast at the individual subject level to compare WM and control conditions, irrespective of load. Contrast images for each participant were then entered in a one-sample test group analysis. Three ROIs were defined, and mean WM-control parameter estimates were calculated for each ROI using MarsBar (Brett et al. 2002). The first ROI corresponded to the whole-brain contrast WM-control corrected for false discovery rate ( $P < 0.05$ ). The other 2 ROIs were 8-mm-radius spheres centered in the left (-31, -54, 46) and right (37, -50, 43) IPS (coordinates from Cohen Kadosh et al. 2008; Fig. 2). ROIs were plotted on a surface-based human atlas (Population-Average, Landmark- and Surface-based (PALS) atlas Van Essen 2005) using the Caret software (Van Essen et al. 2001; <http://www.nitrc.org/projects/caret/>).

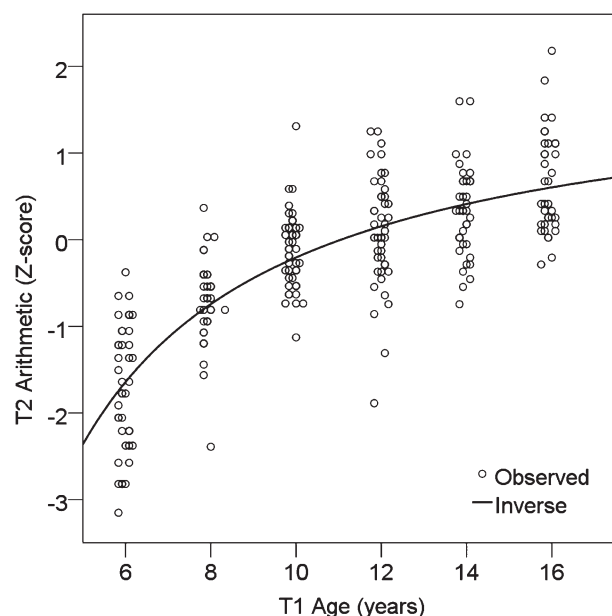
## Results

### Prediction of Arithmetical Performance: Behavioral Measures

A total of 246 participants were included in the behavioral analyses. T1 behavioral measures were scores on the dot matrix, backwards digit, and 3-back WM tasks and on the Raven's matrices reasoning task. Arithmetical performance was the dependent variable assessed at T2. Reasoning and arithmetical scores were preprocessed using IRT to take into account age group differences in items tested, obtaining individual ability scores subsequently transformed into Z-scores (see Bergman Nutley et al. 2010 for details).

In a first step, a curve-fitting analysis was performed to assess how best to model changes in arithmetical performance at T2 as a function of age at T1 (Fig. 1). Linear, logarithmic, and inverse fits were tested, and the results indicated that an inverse function of age at T1 was the best fit for Arithmetic<sub>Z</sub> at T2 ( $R^2 = 0.580, 0.622, \text{ and } 0.642$ , respectively). Age<sup>-1</sup> at T1 was thus the variable entered in all subsequent regression analyses.

Multiple regression analyses were performed comparing a model with T1 Age<sup>-1</sup> only and a model including reasoning and all 3 WM measures at T1. T2 Arithmetic<sub>Z</sub> was the dependent variable. Including the behavioral measures significantly improved the fit of the model. All 4 behavioral measures were found to be significant independent predictors of arithmetical outcome (Table 1). High reasoning and high WM scores at T1 predicted high arithmetical scores at T2.



**Figure 1.** Scatterplot of arithmetical performance of T2 as a function of age at T1. The line represents a fit of the data as a function of Age<sup>-1</sup>, which was found to be a better fit of the development of arithmetical performance than functions of age or ln(age).

**Table 1**

Multiple regression predicting arithmetical performance at T2 using age, reasoning (Raven<sub>Z</sub>), and WM measures (dot matrix, backwards digit, 3-back) in the behavioral sample ( $N = 246$ )

	B	SE	$\beta$
Step 1: $R^2 = 0.642^{***}$			
Constant	1.95	0.11	
T1 Age <sup>-1</sup>	-258.8	12.4	-0.80 <sup>***</sup>
Step 2: $\Delta R^2 = 0.130^{***}$			
Constant	-1.04	0.32	
T1 Age <sup>-1</sup>	-102.2	16.9	-0.32 <sup>***</sup>
T1 Raven <sub>Z</sub>	0.30	0.07	0.21 <sup>***</sup>
T1 dot matrix	0.03	0.01	0.23 <sup>***</sup>
T1 backwards digit	0.03	0.01	0.15 <sup>**</sup>
T1 3-back	0.04	0.01	0.14 <sup>***</sup>

Note: B, beta values;  $\beta$  = standardised beta values; SE = standard error.

\*\* $P < 0.01$ , \*\*\* $P \leq 0.001$ .

A second set of multiple regression analyses were performed to test for possible changes with age in the relationship between the behavioral measures and arithmetical outcome. T1 Age<sup>-1</sup> was transformed into Z-scores to reduce collinearity between main effects and interactions (Aiken and West 1991). T1 Age<sup>-1</sup><sub>Z</sub>, reasoning, and all 3 WM measures at T1 were first entered in the model predicting arithmetical score at T2. In a second stage, interaction terms between T1 Age<sup>-1</sup><sub>Z</sub> and the 4 behavioral measures at T1 were entered in the model. The  $R^2$  change following inclusion of the interaction predictors was not significant ( $\Delta R^2 = 0.006, P = 0.213$ ). Individually, the only significant interaction predictor was the interaction between backwards digit score and T1 Age<sup>-1</sup><sub>Z</sub> ( $\beta = 0.21, P = 0.044$ , all other  $P$ 's  $> 0.24$ ). Thus, the predictive relationship between reasoning and WM measures and arithmetical outcome was mostly stable across the age range (6- to 16-year-olds) of our participants.

### Prediction of Arithmetical Performance: Neuroimaging

A subset of 46 participants were scanned at T1 while performing a visuospatial WM task. The contrast of interest



compared WM conditions (loads 2 or 4) with control conditions matched for stimulus presentation and response production. WM-control mean activation was calculated in the whole-brain WM-control activation ROI and in two 8-mm-radius sphere ROIs centered in the left (-31, -54, 46) and right (37, -50, 43) IPS (coordinates from Cohen Kadosh et al. 2008; Fig. 2).

A first set of regression analyses were performed to test whether WM-control activations were significant predictors of arithmetical outcome irrespective of participants' age. Individually, both whole-brain ROI BOLD and left IPS BOLD at T1 significantly positively predicted arithmetic performance at T2 ( $F_{1,44} = 7.07, P = 0.011, \beta = 0.372, R^2 = 0.138; F_{1,44} = 5.40, P = 0.025, \beta = 0.331, R^2 = 0.109$ , respectively). There was a trend for a similar effect for the right IPS BOLD at T1 ( $F_{1,44} = 2.84, P = 0.099, \beta = 0.372, R^2 = 0.061$ ).

We then performed a set of multiple regressions where T1 Age<sup>-1</sup> was entered first in the model, the whole-brain ROI activation second, and then either the right or the left IPS ROI activations. This approach enabled us to assess specific IPS effects once overall brain activation and age were taken into account. The left IPS independently explained a significant amount (5.1%) of additional variance in T2 Arithmetic<sub>Z</sub> (Table 2). Greater left IPS residual activation once the effect of age was taken into account was associated with poorer arithmetical performance 2 years later. In this case, the right IPS was not a significant predictor of arithmetical outcome ( $\Delta R^2 = 0.003, P > 0.5$ ).

Similarly to the behavioral analyses, additional multiple regression analyses of the functional MRI (fMRI) data were performed to test for possible changes with age in the relationship between the left IPS and whole-brain BOLD measures and arithmetical outcome. T1 Age<sup>-1</sup><sub>Z</sub> and whole-brain and left IPS WM-control BOLD at T1 were first entered in the model. In a second stage, interaction terms between T1 Age<sup>-1</sup><sub>Z</sub> and the 2 BOLD measures at T1 were entered in the model. The R<sup>2</sup> change following inclusion of the interaction predictors was not significant ( $\Delta R^2 = 0.007, P = 0.592$ ,

individual interaction predictor  $P$ 's > 0.3). Thus, the predictive relationship between whole-brain and left IPS BOLD measures and arithmetical outcome appeared stable across the age range (6- to 16-year-olds) of our participants.

A second set of multiple regression analyses assessed the significance of the WM and reasoning behavioral measures in the smaller neuroimaging sample of participants and tested whether the left IPS effect remained significant when behavioral measures were first included in the model. Results showed that in this smaller sample, behavioral measures explained 10.1% more variance than age only. Only the reasoning and visuospatial WM measures significantly contributed to the model (Table 3). Importantly, adding activation in the left IPS to the model after whole-brain activation was included led to a further significant improvement of the full regression model of 2.5% (Table 3).

### Identification of the 20% Lower Performers

As an illustration of the added benefit of using neuroimaging data as a predictor of arithmetical outcome, we classified the

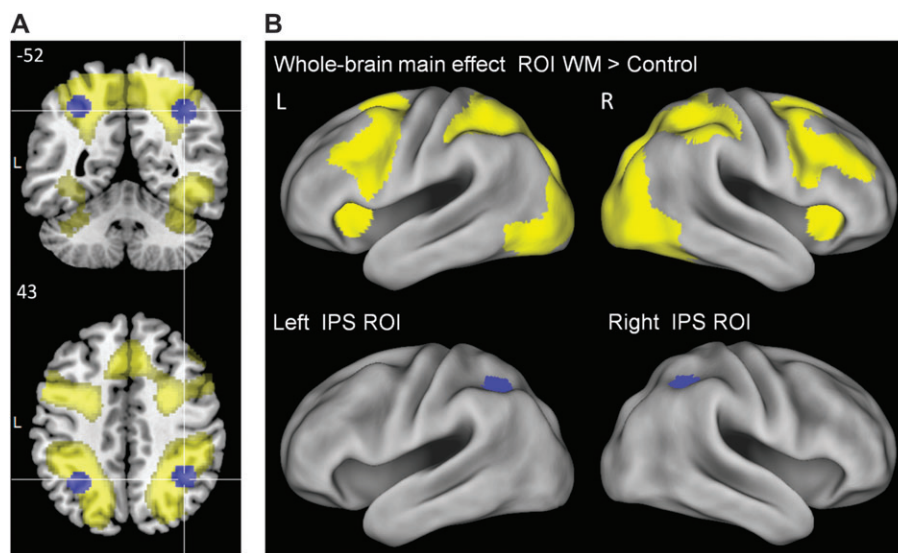
**Table 2**

Multiple regression predicting arithmetical performance at T2 using age and whole-brain and left IPS WM-control ROIs mean activation in the fMRI sample ( $N = 46$ )

	<i>B</i>	SE	$\beta$
Step 1: $R^2 = 0.687^{***}$			
Constant	1.68	0.18	
T1 Age <sup>-1</sup>	-199.8	20.3	-0.83 <sup>***</sup>
Step 2: $\Delta R^2 = 0.003$			
Constant	1.79	0.25	
T1 Age <sup>-1</sup>	-207.6	23.7	-0.86 <sup>***</sup>
T1 whole-brain WM-control	-0.13	0.19	-0.06
Step 3: $\Delta R^2 = 0.051^{**}$			
Constant	2.02	0.25	
T1 Age <sup>-1</sup>	-229.8	23.3	-0.95 <sup>***</sup>
T1 whole-brain WM-control	0.50	0.28	0.26 <sup>†</sup>
T1 left IPS WM-control	-0.51	0.18	-0.44 <sup>***</sup>

Note: *B*, beta values;  $\beta$  = standardised beta values; SE = standard error.

<sup>†</sup> $P < 0.1$ , <sup>\*\*</sup> $P < 0.01$ , <sup>\*\*\*</sup> $P \leq 0.001$ .



**Figure 2.** Representation of the ROIs used in the fMRI analyses. (A) Coronal and transverse slices: The whole-brain contrast of the WM-control conditions is represented in yellow and was performed using False Discovery Rate (FDR) correction ( $P < 0.05$ ); the IPS ROIs are represented in blue and were 8-mm-radius spheres centered on coordinates obtained by Cohen Kadosh et al. (2008) in a meta-analysis of fMRI studies of numerical representation (left IPS: -31, -54, 46; right IPS: 37, -50, 43). (B) Render of the whole-brain main effect and IPS ROIs on a surface-based human atlas (see Materials and Methods).

**Table 3**

Multiple regression predicting arithmetical performance at T2 using age, reasoning, and WM behavioral measures and whole-brain and left IPS WM-control ROIs mean activation in the fMRI sample ( $N = 46$ )

	Step 1: $R^2 = 0.687$			Step 2: $\Delta R^2 = 0.101^{**}$			Step 3: $\Delta R^2 = 0.001$			Step 4: $\Delta R^2 = 0.025^*$		
	<i>B</i>	SE	$\beta$	<i>B</i>	SE	$\beta$	<i>B</i>	SE	$\beta$	<i>B</i>	SE	$\beta$
Constant	1.68	0.18		0.57	0.94		0.7	1.03		0.64	0.98	
T1 Age <sup>-1</sup>	-199.8	20.3	-0.83***	-107.5	31.6	-0.45**	-113.5	36.8	-0.47**	-139.9	37.0	-0.58***
T1 Raven <sub>z</sub>				0.24	0.10	0.27*	0.23	0.11	0.27*	0.16	0.11	0.18
T1 dot matrix				0.04	0.01	0.37**	0.04	0.01	0.37**	0.04	0.01	0.36**
T1 backwards digit				-0.02	0.02	-0.11	-0.02	0.02	-0.11	-0.02	0.01	-0.11
T1 3-back				-0.02	0.04	-0.05	-0.02	0.04	-0.05	-0.00	0.04	-0.01
T1 whole-brain WM-control							-0.06	0.18	-0.03	0.40	0.27	0.20
T1 left IPS WM-control										-0.38	0.17	-0.33*

Note: *B*, beta values;  $\beta$  = standardised beta values; SE = standard error.

\* $P < 0.05$ , \*\* $P < 0.01$ , \*\*\* $P \leq 0.001$ .

fMRI sample into the 20% lower T2 Arithmetic<sub>z</sub> performers and 80% better performers per age group (6-, 8-, 10-, 12-, 14-, or 16-year-olds at T1). The 20% threshold was chosen as an intermediary value between the 25% poor functional numeracy observed in adults (Parsons and Bynner 2005) and the 15% cutoff used for mathematics learning disability (MLD) in elementary school children (Geary et al. 2009). Binary logistic regression analyses were performed on these data to assess how well our models could classify the participants in these 2 categories. Sensitivity represents the proportion of lower 20% performers correctly identified as low performers and specificity the proportion of higher 80% performers correctly identified as high performers.

A model including age and all behavioral measures did not classify the participants better (trend only:  $\chi^2_4 = 8.6$ ,  $P = 0.073$ , sensitivity 22.2%, specificity 97.3%, accuracy 82.6%) than a model with age alone (sensitivity 0%, specificity 100%, accuracy 80.4%). However, including whole-brain and left IPS WM-control activity made a significant improvement to the model ( $\chi^2_2 = 6.5$ ,  $P = 0.039$ ), with the final full model (including behavioral and BOLD measures) classifying the participants in this smaller group significantly better than the model with age alone ( $\chi^2_6 = 15.1$ ,  $P = 0.020$ , sensitivity 55.6%, specificity 94.6%, accuracy 87.0%). Adding fMRI measures to the model led to the correct classification of 5 of 9 low performers instead of 2 of 9 when using the behavioral measures only.

## Discussion

This longitudinal study combined behavioral and brain imaging measures to test whether functional imaging data could improve prediction of arithmetical outcome in 6- to 16-year-old participants. Our results show that greater activation in the left, but not right, IPS during a visuospatial WM task relative to the rest of the brain is associated with poorer arithmetical performance 2 years later. Left IPS activity is still a significant, although small, predictor when WM and reasoning abilities are first entered as predictors of arithmetical outcome. Although the participant samples were small, the use of brain imaging data improved more than 2-fold the accurate classification of participants as poor arithmetical performers 2 years later. These results provide initial evidence that brain imaging is a sensitive tool for the identification of children at risk of poor academic outcome.

Developmental changes in arithmetical performance could be fitted by an inverse function of age, with the steepest improvements in performance observed between participants

aged 6 and 8 at T1. A large part of the variance in arithmetical performance in our sample (64.2%) was predicted by Age<sup>-1</sup>. In this aspect, the present study differs from previous longitudinal research in that a wide age range was included in the analyses instead of focusing on a single age group (Gathercole et al. 2003; Bull et al. 2008; Alloway TP and Alloway RG 2010) or using age-corrected measures (Bull et al. 2008). In line with previous longitudinal data (see Raghobar et al. 2010 for review), WM and reasoning abilities were found to be significant predictors of arithmetical outcome. Here, reasoning and all 3 WM measures were unique predictors of arithmetical performance 2 years later, accounting together for an additional 13% of variance when age was first entered in the model. These results fit with previous findings of unique contributing effects of WM and nonverbal IQ (Alloway TP and Alloway RG 2010) and verbal and visuospatial WM (Bull et al. 2008) for the prediction of mathematical outcome and extend the findings to a wide developmental age range. Overall, there was little evidence for a change with age in the relationship between the behavioral predictors and arithmetical outcome. Our findings thus suggest a consistent association between WM and reasoning measures and arithmetical abilities throughout childhood and adolescence.

In the smaller fMRI sample, only reasoning and visuospatial WM were significant predictors of arithmetical score at T2, which suggests verbal WM may be less strongly associated with arithmetical performance. In line with these results, verbal WM measures at age 4 have been found to predict reading comprehension, writing, and spelling, but not mathematics, 2.5 years later (Gathercole et al. 2003) and to predict mathematical performance at the entrance but not at the end of the first or third years of primary school (Bull et al. 2008; see also Meyer et al. 2010). Note that, possibly counterintuitively, those verbal WM measures that were less strongly associated with arithmetical performance 2 years later in our sample, the backwards digit and 3-back tasks, were those that involved some aspect of numerical representation. Indeed, it could be argued that although the 3-back task required maintaining and updating nonnumerical Swedish words in WM, participants needed to count until 3 to perform the task accurately.

These results overall support the use of WM measures, in particular visuospatial WM, for the early identification of children at risk of poor academic outcome in arithmetic. WM training programs (Klingberg 2010) have been shown to improve clinical symptoms of psychiatric disorders such as ADHD (Klingberg et al. 2002b, 2005), as well as performance on tests of mathematics, with mathematical reasoning

improvements observed 6 months after WM training (Holmes et al. 2009). Previous mathematics training studies have focused on specific number-related training and obtained mixed results: Training using number- versus color-based board games led to improvements in performance of a range of numerical tasks at the end of training and 9 weeks later (Ramani and Siegler 2008), while training on computerized tasks emphasizing either numerical comparison or small exact numerosities showed improvement in number comparison but not counting or arithmetic after the training and 3 weeks later (Räsänen et al. 2009).

The main aim of the current study was to investigate whether brain-imaging measures of WM would complement typical behavioral assessments and contribute uniquely to the prediction of arithmetical outcome. The analyses focused on the IPS, a brain region that has been specifically implicated in both numerical processing (Dehaene et al. 2003; Cohen Kadosh et al. 2008) and visuospatial WM (Linden 2007) and where visuospatial WM and arithmetical tasks show overlapping activity (Zago and Tzourio-Mazoyer 2002; Zago et al. 2008). IPS activation during number processing tasks correlates with arithmetical or mathematical abilities (Rubinsten and Henik 2009; Butterworth 2010), and IPS activation during visuospatial WM tasks correlates with WM capacity (Klingberg et al. 2002a; Todd and Marois 2005; Crone et al. 2006). However, there is no previous evidence that WM activation in the IPS may be directly linked to arithmetical performance. Instead, different neural populations may underlie the activations observed in visuospatial WM and number processing tasks. The present study argues against this by showing that neural activity during visuospatial WM tasks in the IPS has predictive value for the development of arithmetical abilities.

Our results first indicated that greater activation in the whole-brain WM-control network, in the left IPS or in the right IPS (although at trend level only), predicted better arithmetical performance 2 years later. These results are broadly consistent with those of Rotzer et al. (2009), which showed that poor arithmetical abilities were associated with weaker right IPS activation during a spatial WM task in 8- to 10-year-old children. When the age of the participants was included in our analyses, the results showed that in combination with whole-brain activity, left IPS activity during a visuospatial WM task predicted 5% more variance in arithmetical performance 2 years later than age alone. There was no significant interaction between the BOLD predictors and age, suggesting the observed effects were consistent across the age range of the participants. Further, whole-brain activity and left IPS activity predicted 2.5% more variance than age and the behavioral reasoning and WM measures. Interestingly, in the full regression models, the only significant predictors were Age<sup>-1</sup>, visuospatial WM, and left IPS activity during the visuospatial WM task, highlighting the specifically high association between visuospatial WM and arithmetical performance.

When age was taken into account as a predictor, greater activation in the left IPS was thus associated with poorer arithmetical performance 2 years later, while there was a trend for greater activation in the whole-brain ROI to be associated with better arithmetical outcome. This direction of the IPS association, and its hemispheric localization, differs from the findings of Rotzer et al. (2009). However, in their study, age was not taken into account. It is possible that age effects on the WM activation in the right IPS might have affected the observed

positive correlation between right IPS WM activation and arithmetical performance observed by Rotzer et al. (2009). The direction of the left IPS residual effect observed in the current study is novel and will need to be investigated further. It is possible that a complex pattern of relative activation levels in the different brain regions of the WM network is what is relevant for predicting arithmetical outcome. Such a pattern may be behind the present finding that when age is covaried, weaker left IPS activation, in the context of a greater whole-brain network WM activation, is associated with better arithmetical outcome.

A potential limitation of these results lies in the fact that the visuospatial WM task in the scanner included the presentation of a single digit number in the response phase of the task. It is thus possible that the association between IPS activation during the task and arithmetical performance 2 years later partly reflects the processing of numerical representation in the response phase. Indeed, both spoken and written numerals have been shown to specifically activate the IPS (Naccache and Dehaene 2001; Eger et al. 2003). However, the control condition of the visuospatial WM task also included the presentation of a single digit number, which should have reduced this potential confound, and suggests that the findings observed here may be specific to visuospatial WM activation.

To test a potential application of these results, we performed additional analyses that showed that age and behavioral measures could correctly classify only 2 of 9 of the 20% lower arithmetical performers, while adding fMRI WM data to the model improved this classification more than 2-fold to 5 of 9. Although the sample sizes were small, these results suggest that fMRI data can be used to improve the identification of individuals at risk of future low academic performance in the domain of mathematics. This study thus extends previous research showing that brain measures (event-related potentials) could identify infants and young children at risk for dyslexia (Maurer et al. 2009; Guttorm et al. 2010; see Gabrieli 2009 for review) and provides further support for the usefulness of neuroimaging data. It remains to be seen which fMRI cognitive task would best predict arithmetical outcome. A combination of brain activation during a numerical processing task and numerical performance measures outside the scanner may have the best predictive power. However, an advantage of WM tasks is that they do not require number knowledge and could thus be performed, and trained, at an earlier age.

Underlying the link between visuospatial WM and arithmetical abilities may be their reliance on a common spatial “memory map.” In nonhuman primates, visuospatial information is assumed to be kept in WM by sustained activity in neurons coding specifically for stimuli at different visual angles (Funahashi et al. 1989). In humans, neural specificity for the visuospatial location of stimuli can be demonstrated by showing retinotopic organization in a cortical region. Retinotopy has been found both in the IPS and in the frontal eye field during the delay period of a visuospatial WM task (Konen and Kastner 2008; Silver and Kastner 2009). Such a spatial memory map could also be used for an analog spatial representation of numbers, and there is indeed evidence of spatial aspects of the representation of numbers. Behavioral data suggest that number comparison is performed using a mental number line, an analog spatial representation in which numerical magnitude is represented along an axis oriented according to the direction of writing (Dehaene et al. 1993). This representation enhances responses to number stimuli whose values accord with the



spatial position of the response (spatial and numerical association of response codes task; Dehaene et al. 1993) and induces corresponding left/right shifts of attention (Nicholls et al. 2008). There is evidence in early development for a number-space mapping (de Hevia and Spelke 2010) and a general magnitude representation shared between the dimensions of space, number, and time (Lourenco and Longo 2010). In adults, a common frontoparietal network supporting processing of these 3 dimensions has been proposed (Walsh 2003) and is supported by studies showing that all 3 dimensions are similarly affected by saccadic compression (Burr et al. 2010). Thus, the spatial mapping required by visuospatial WM tasks and the mental number line mapping required by number comparison and arithmetical tasks may recruit similar neural populations.

Although the effects were small, the fact that neuroimaging data could significantly improve arithmetical outcome prediction compared with behavioral measures may be related to the intermediate phenotypes concept put forwards in the imaging genetics literature (Meyer-Lindenberg and Weinberger 2006). The suggestion is that neuroimaging measures may be more sensitive to individual differences by being closer to the biological substrate. Dyscalculia and poor performance in arithmetic are quite specifically associated with dysfunction of the IPS. Imaging data, which contrasts well-matched conditions in terms of visual stimuli and motor responses, can provide information on a subpart of the components that add to a behavioral WM score, for example, processes of maintenance of information over a delay, and can provide localized measures of corresponding brain function. In addition, imaging data may reflect physiological or neural properties that might provide information about future capacity, for example, number of neurons, or measures of structural maturity (synaptic connectivity strength and myelination), which are the basis of future cognitive development. In the present study, IPS activation during visuospatial WM may thus reflect the potential of local neural resources for supporting future arithmetical development.

Note that, although our participants were overall typically developing, it is likely that our results have validity for children with larger arithmetical deficits or dyscalculia as it has been suggested that the genetic components of MLD are likely to be the same as those underlying individual differences in mathematics achievement (Kovas et al. 2007). Moreover, the results obtained here in a large age range suggest that some behavioral and brain measures are good predictors of future arithmetical performance throughout development. Further work may identify whether some measures may be more specific to young age groups, for the development of tests permitting the early identification of children at risk of poor arithmetical outcome.

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## References

- Aiken LS, West SG. 1991. Multiple regression: testing and interpreting interactions. Newbury Park (CA): Sage.
- Alloway TP. 2007. Automated Working Memory Assessment Manual. Oxford: Harcourt.
- Alloway TP, Alloway RG. 2010. Investigating the predictive roles of working memory and IQ in academic attainment. *J Exp Child Psychol.* 106:20-29.
- Alloway TP, Gathercole SE, Adams A-M, Willis C, Eaglen R, Lamont E. 2005. Working memory and phonological awareness as predictors of progress towards early learning goals at school entry. *Brit J Dev Psychol.* 23:417-426.
- Alloway TP, Gathercole SE, Kirkwood H, Elliott J. 2009. The cognitive and behavioral characteristics of children with low working memory. *Child Dev.* 80:606-621.
- American Psychiatric Association 2000. Diagnostic and Statistical Manual of Mental Disorders. Revised 4th ed. Washington (DC): American Psychiatric Association.
- Andersson U. 2010. Skill development in different components of arithmetic and basic cognitive functions: findings from a 3-year longitudinal study of children with different types of learning difficulties. *J Educ Psychol.* 102:115-134.
- Berch DB. 2008. Working memory and mathematical cognitive development: limitations of limited-capacity resource models. *Dev Neuropsychol.* 33:427-446.
- Bergman Nutley S, Soderqvist S, Bryde S, Humphreys K, Klingberg T. 2010. Measuring working memory capacity with greater precision in the lower capacity ranges. *Dev Neuropsychol.* 35:81-95.
- Brett M, Valabregue R, Poline J-B. 2002. Region of interest analysis using an SPM toolbox [abstract]. Eighth International Conference on Functional Mapping of the Human Brain, June 2-6 2002, Sendai, Japan.
- Bull R, Espy KA, Wiebe SA. 2008. Short-term memory, working memory, and executive functioning in preschoolers: longitudinal predictors of mathematical achievement at age 7 years. *Dev Neuropsychol.* 33:205-228.
- Burr DC, Ross J, Binda P, Morrone MC. 2010. Saccades compress space, time and number. *Trends Cogn Sci.* 14:528-533.
- Butterworth B. 2005. The development of arithmetical abilities. *J Child Psychol Psych.* 46:3-18.
- Butterworth B. 2010. Foundational numerical capacities and the origins of dyscalculia. *Trends Cogn Sci.* 14:534-541.
- Cohen Kadosh R, Lammertyn J, Izard V. 2008. Are numbers special? An overview of chronometric, neuroimaging, developmental and comparative studies of magnitude representation. *Progr Neurobiol.* 84:132-147.
- Crone EA, Wendelken C, Donohue S, Van LL, Bunge SA. 2006. Neurocognitive development of the ability to manipulate information in working memory. *Proc Natl Acad Sci U S A.* 103:9315-9320.
- de Hevia MD, Spelke ES. 2010. Number-space mapping in human infants. *Psychol Sci.* 21:653-660.
- Dehaene S, Bossini S, Giraux P. 1993. The mental representation of parity and number magnitude. *J Exp Psychol Gen.* 122:371-396.
- Dehaene S, Molko N, Cohen L, Wilson AJ. 2004. Arithmetic and the brain. *Curr Opin Neurobiol.* 14:218-224.
- Dehaene S, Piazza M, Pinel P, Cohen L. 2003. Three parietal circuits for number processing. *Cogn Neuropsychol.* 20:487-506.
- Eger E, Sterzer P, Russ MO, Giraud A-L, Kleinschmidt A. 2003. A supramodal number representation in human intraparietal cortex. *Neuron.* 37:719-725.
- Funahashi S, Bruce CJ, Goldman-Rakic PS. 1989. Mnemonic coding of visual space in the monkey's dorsolateral prefrontal cortex. *J Neurophysiol.* 6:331-349.
- Gabrieli JDE. 2009. Dyslexia: a new synergy between education and cognitive neuroscience. *Science.* 325:280-283.
- Gathercole SE, Brown L, Pickering SJ. 2003. Working memory assessments at school entry as longitudinal predictors of National Curriculum attainment levels. *Educ Child Psychol.* 20:109-122.

- Geary DC, Bailey DH, Hoard MK. 2009. Predicting mathematical achievement and mathematical learning disability with a simple screening tool: the number sets test. *J Psychoeduc Assess.* 27:265-279.
- Gersten R, Jordan NC, Flojo JR. 2005. Early identification and interventions for students with mathematics difficulties. *J Learn Disabil.* 38:293-304.
- Gillham B, Hesse K. 2001. *Basic Number Screening Test*. London: Hodder and Stoughton International.
- Gross J, Hudson C, Price D. 2009. *The long term costs of numeracy difficulties*. London (UK): Every Child a Chance Trust and KPMG.
- Guttorm TK, Leppänen PHT, Hämäläinen JA, Eklund KM, Lyytinen HJ. 2010. Newborn event-related potentials predict poorer pre-reading skills in children at risk for dyslexia. *J Learn Disabil.* 43:391-401.
- Henry LA, MacLean M. 2003. Relationships between working memory, expressive vocabulary and arithmetical reasoning in children with and without intellectual disabilities. *Educ Child Psychol.* 20:51-64.
- Holmes J, Gathercole SE, Dunning DL. 2009. Adaptive training leads to sustained enhancement of poor working memory in children. *Dev Sci.* 12:F9-F15.
- Isaacs EB, Edmonds CJ, Lucas A, Gadian DG. 2001. Calculation difficulties in children of very low birth weight: a neural correlate. *Brain.* 124:1701-1707.
- Jarvis HL, Gathercole SE. 2003. Verbal and non-verbal working memory and achievements on National Curriculum tests at 11 and 14 years of age. *Educ Child Psychol.* 20:123-140.
- Kaufmann L, Vogel SE, Starke M, Kremser C, Schocke M, Wood G. 2009. Developmental dyscalculia: compensatory mechanisms in left intraparietal regions in response to nonsymbolic magnitudes. *Behav Brain Funct.* 5:35.
- Klingberg T. 2010. Training and plasticity of working memory. *Trends Cogn Sci.* 14:317-324.
- Klingberg T, Fernell E, Olesen PJ, Johnson M, Gustafsson P, Dahlström K, Gillberg CG, Forssberg H, Westerberg H. 2005. Computerized training of working memory in children with ADHD—a randomized, controlled trial. *J Am Acad Child Psy.* 44:177-186.
- Klingberg T, Forssberg H, Westerberg H. 2002a. Increased brain activity in frontal and parietal cortex underlies the development of visuospatial working memory capacity during childhood. *J Cogn Neurosci.* 14:1-10.
- Klingberg T, Forssberg H, Westerberg H. 2002b. Training of working memory in children with ADHD. *J Clin Exp Neuropsychol.* 24:781-791.
- Konen CS, Kastner S. 2008. Representation of eye movements and stimulus motion in topographically organized areas of human posterior parietal cortex. *J Neurosci.* 28:8361-8375.
- Kovas Y, Haworth CMA, Dale PS, Plomin R. 2007. The genetic and environmental origins of learning abilities and disabilities in the early school years. *Monogr Soc Res Child Dev.* 72(3):60-66.
- Kucian K, Loenneker T, Dietrich T, Dosch M, Martin E, von Aster M. 2006. Impaired neural networks for approximate calculation in dyscalculic children: a functional MRI study. *Behav Brain Funct.* 2:31.
- Kyttälä M, Aunio P, Lehto JE, Luit JV. 2003. Visuospatial working memory and early numeracy. *Educ Child Psychol.* 20:65-76.
- Linden DEJ. 2007. The working memory networks of the human brain. *Neuroscientist.* 13:257-267.
- Lourenco SF, Longo MR. 2010. General magnitude representation in human infants. *Psychol Sci.* 21:873-881.
- Martin M, Mullis S, Chrostowski S, editors. *TIMSS 2003 Technical Report*. Chestnut Hill (MA): TIMSS & PIRLS International Study Centre Boston College.
- Maurer U, Bucher K, Brem S, Benz R, Kranz F, Schulz E, van der Mark S, Steinhausen H-C, Brandeis D. 2009. Neurophysiology in preschool improves behavioral prediction of reading ability throughout primary school. *Biol Psychiat.* 66:341-348.
- Maybery MT, Do N. 2003. Relationships between facets of working memory and performance on a curriculum-based mathematics test in children. *Educ Child Psychol.* 20:77-92.
- Meyer ML, Salimpoor VN, Wu SS, Geary DC, Menon V. 2010. Differential contribution of specific working memory components to mathematics achievement in 2nd and 3rd graders. *Learn Individ Differ.* 20:101-109.
- Meyer-Lindenberg A, Weinberger DR. 2006. Intermediate phenotypes and genetic mechanisms of psychiatric disorders. *Nat Rev Neurosci.* 7:818-827.
- Mussolin C, De Volder A, Grandin C, Schlögel X, Nassogne M-C, Noël M-P. 2010. Neural correlates of symbolic number comparison in developmental dyscalculia. *J Cogn Neurosci.* 22:860-874.
- Naccache L, Dehaene S. 2001. The priming method: imaging unconscious repetition priming reveals an abstract representation of number in the parietal lobes. *Cereb Cortex.* 11:966-974.
- Nicholls MER, Loftus AM, Gevers W. 2008. Look, no hands: a perceptual task shows that number magnitude induces shifts of attention. *Psychon Bull Rev.* 15:413-418.
- Parsons S, Bynner J. 2005. *Does numeracy matter more?* London: National Research and Development Centre for Adult Literacy and Numeracy, Institute of Education.
- Passolunghi M, Vercelloni B, Schadee H. 2007. The precursors of mathematics learning: working memory, phonological ability and numerical competence. *Cogn Dev.* 22:165-184.
- Price GR, Holloway I, Räsänen P, Vesterinen M, Ansari D. 2007. Impaired parietal magnitude processing in developmental dyscalculia. *Curr Biol.* 17:R1042-R1043.
- Primi R, Ferrão ME, Almeida LS. 2010. Fluid intelligence as a predictor of learning: a longitudinal multilevel approach applied to math. *Learn Individ Differ.* 20:446-451.
- Raghubar KP, Barnes MA, Hecht SA. 2010. Working memory and mathematics: a review of developmental, individual difference, and cognitive approaches. *Learn Individ Differ.* 20:110-122.
- Ramani GB, Siegler RS. 2008. Promoting broad and stable improvements in low-income children's numerical knowledge through playing number board games. *Child Dev.* 79:375-394.
- Räsänen P, Salminen J, Wilson AJ, Aunio P, Dehaene S. 2009. Computer-assisted intervention for children with low numeracy skills. *Cogn Dev.* 24:450-472.
- Rasmussen C, Bisanz J. 2005. Representation and working memory in early arithmetic. *J Exp Child Psychol.* 91:137-157.
- Raven JC. 1998. *Manual for Raven's progressive matrices*. Oxford: Oxford Psychologists Press.
- Rotzer S, Kucian K, Martin E, von Aster M, Klaver P, Loenneker T. 2008. Optimized voxel-based morphometry in children with developmental dyscalculia. *Neuroimage.* 39:417-422.
- Rotzer S, Loenneker T, Kucian K, Martin E, Klaver P, von Aster M. 2009. Dysfunctional neural network of spatial working memory contributes to developmental dyscalculia. *Neuropsychologia.* 47:2859-2865.
- Rubinsten O, Henik A. 2009. Developmental dyscalculia: heterogeneity might not mean different mechanisms. *Trends Cogn Sci.* 13:92-99.
- Rykhlevskaia E, Uddin LQ, Kondos L, Menon V. 2009. Neuroanatomical correlates of developmental dyscalculia: combined evidence from morphometry and tractography. *Front Hum Neurosci.* 3:51.
- Silver MA, Kastner S. 2009. Topographic maps in human frontal and parietal cortex. *Trends Cogn Sci.* 13:488-495.
- Söderqvist S, McNab F, Peyrard-Janvid M, Matsson H, Humphreys K, Kere J, Klingberg T. 2010. The SNAP25 gene is linked to working memory capacity and maturation of the posterior cingulate cortex during childhood. *Biol Psychiat.* 68:1120-1125.
- Todd JJ, Marois R. 2005. Posterior parietal cortex activity predicts individual differences in visual short-term memory capacity. *Cogn Affec Behav Neurosci.* 5:144-155.
- Van Essen DC. 2005. A Population-Average, Landmark- and Surface-based (PALS) atlas of human cerebral cortex. *Neuroimage.* 28:635-662.
- Van Essen DC, Drury HA, Dickson J, Harwell J, Hanlon D, Anderson CH. 2001. An integrated software suite for surface-based analyses of cerebral cortex. *J Am Med Inform Assn.* 8:443-459.
- Walsh V. 2003. A theory of magnitude: common cortical metrics of time, space and quantity. *Trends Cogn Sci.* 7:483-488.
- Zago L, Petit L, Turbelin M-R, Andersson F, Vigneau M, Tzourio-Mazoyer N. 2008. How verbal and spatial manipulation networks contribute to calculation: an fMRI study. *Neuropsychologia.* 46:2403-2414.
- Zago L, Tzourio-Mazoyer N. 2002. Distinguishing visuospatial working memory and complex mental calculation areas within the parietal lobes. *Neurosci Lett.* 331:45-49.